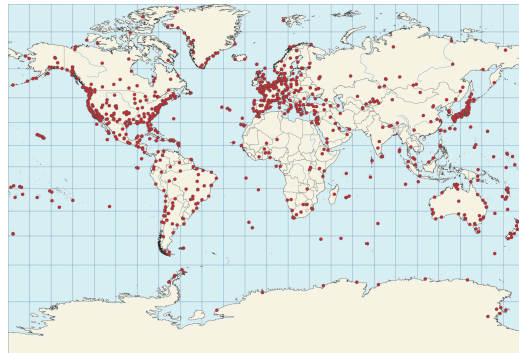


# LAGEOS: Importance to the Reference Frame, Enabled Missions, Future Outlook



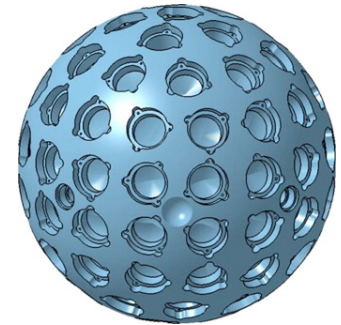
LAGEOS 1,2



(e.g.) ITRF2014



Altimeter satellites



LARES

*Frank G. Lemoine*  
**“40 Years of Reflections”**  
**(40<sup>th</sup> Anniversary LAGEOS celebration)**  
*Planetary Geodynamics Laboratory, Code 698*  
*NASA Goddard Space Flight Center*  
*May 11, 2016*

# Reference Frame: What is it?

**SLR**



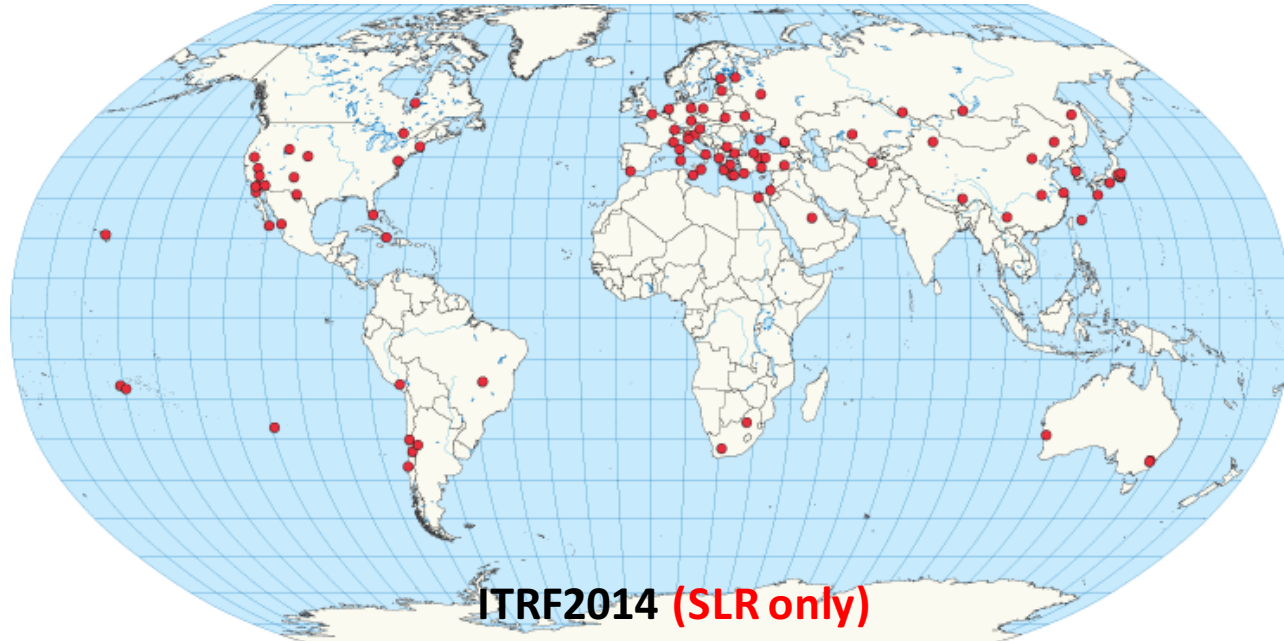
e.g. Hartbeesthoek

+

**GPS**



e.g. Greenbelt



ITRF2014 (SLR only)

+ **VLBI**



e.g. Greenbelt

+

**DORIS**



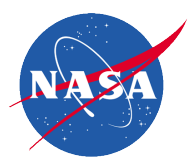
e.g. Yarragadee

+

**site ties**

=

an ITRF  
Realization,  
e.g.  
ITRF2014

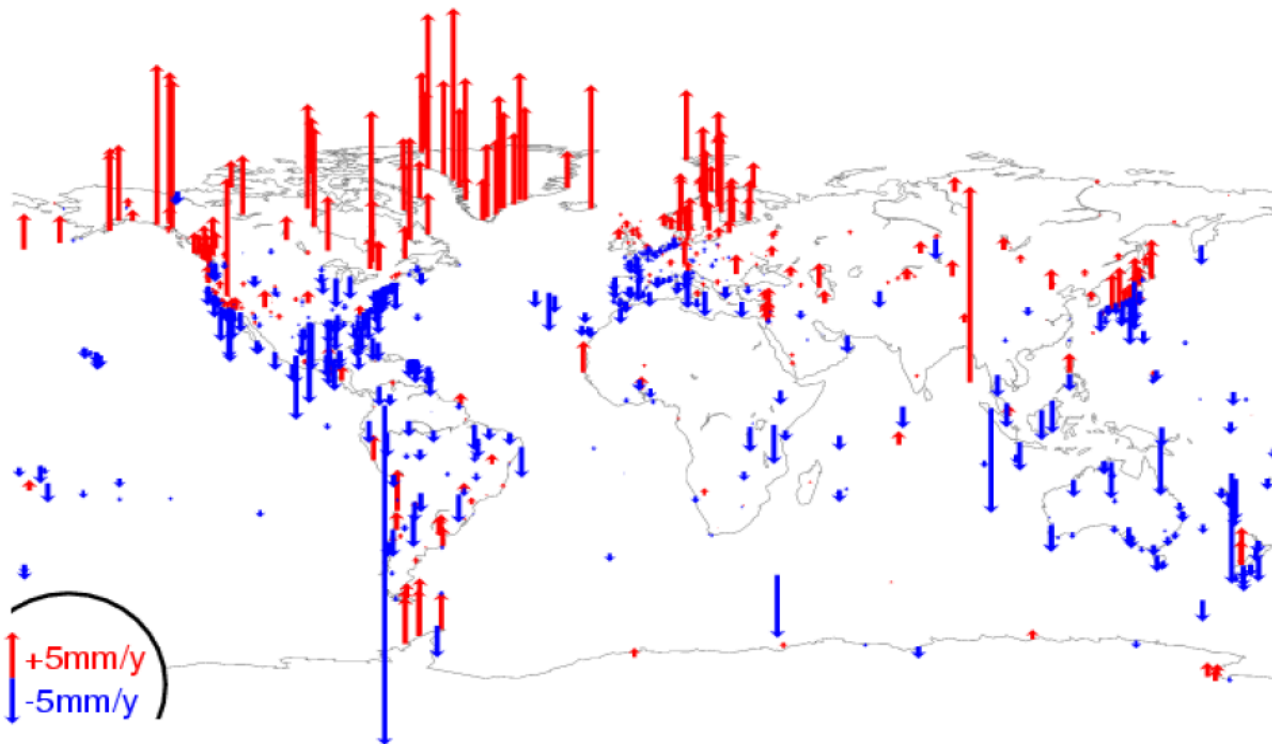
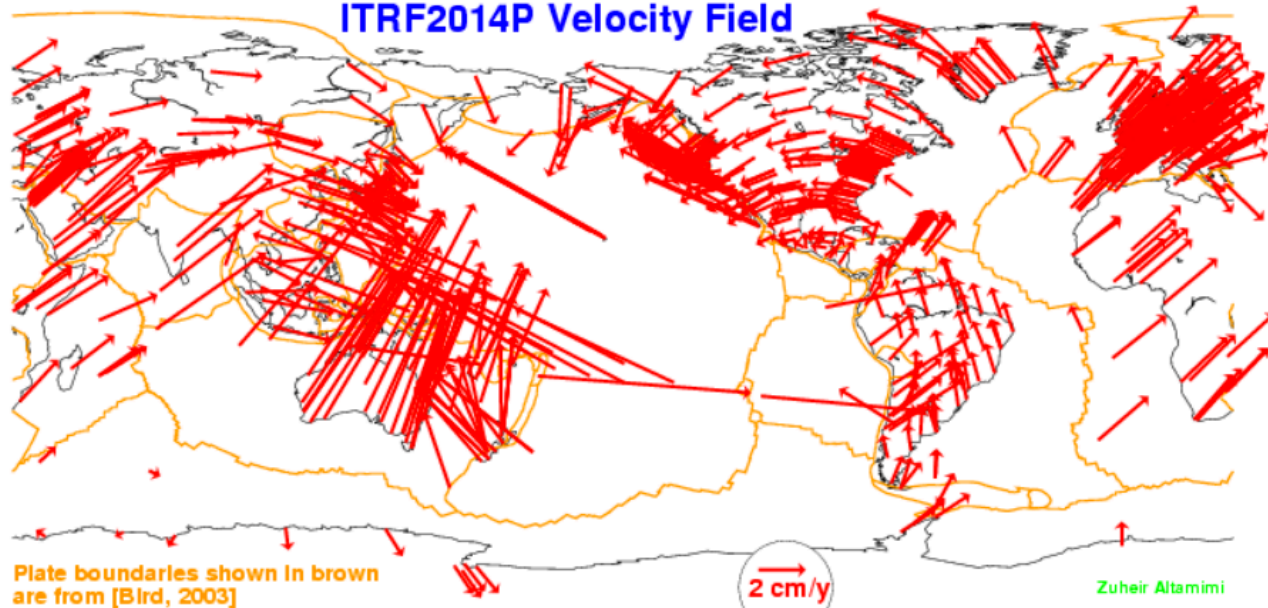


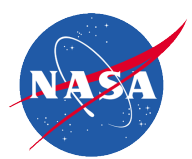
A reference frame realization consists of **positions and velocities of the reference points.**

For ITRF2014, post-seismic relaxation is also modeled for the first time.

Figures from Zuheir Altamimi, IGN/France

### ITRF2014P Velocity Field





# ILRS/SLR origin components wrt. ITRF2014

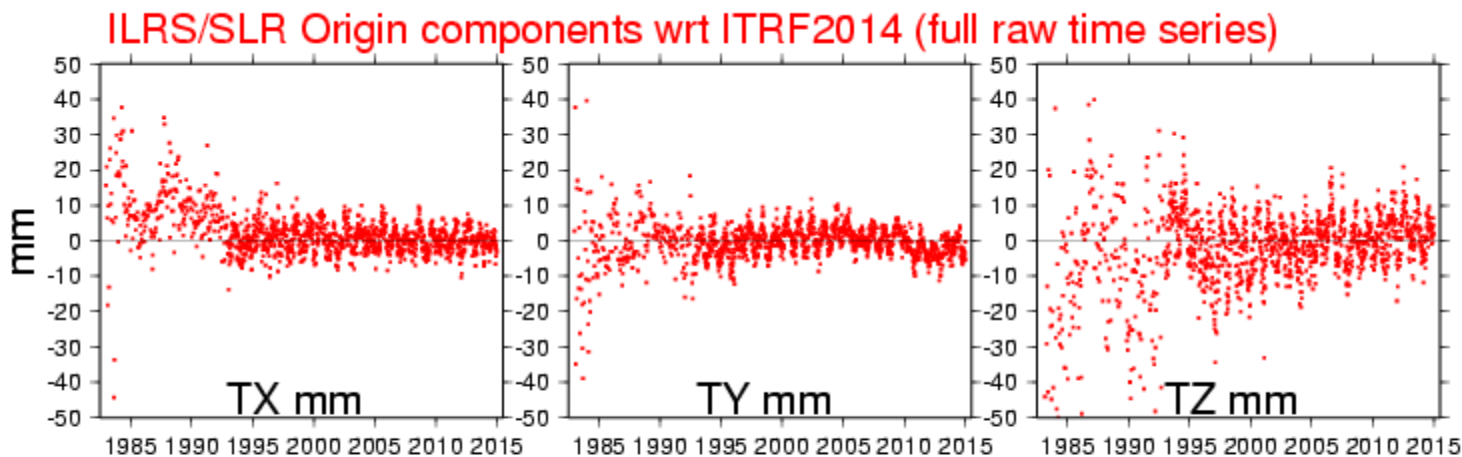
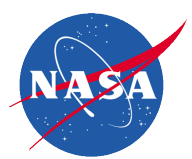


Figure from Zuheir Altamimi, IGN/France  
(Altamimi et al., 2016)



# ILRS/SLR origin components wrt. ITRF2014

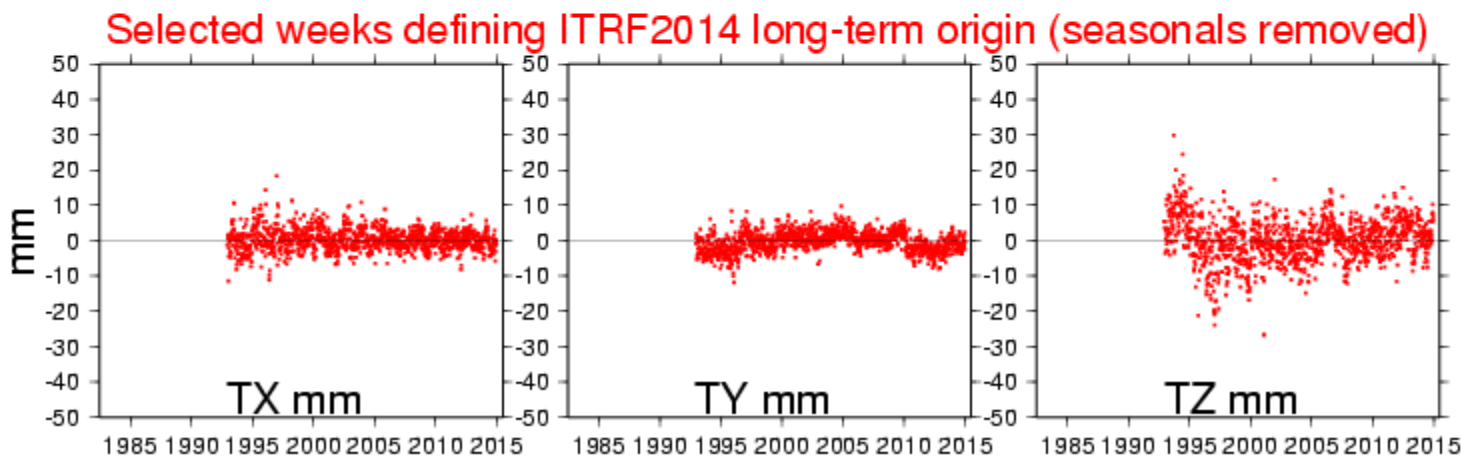
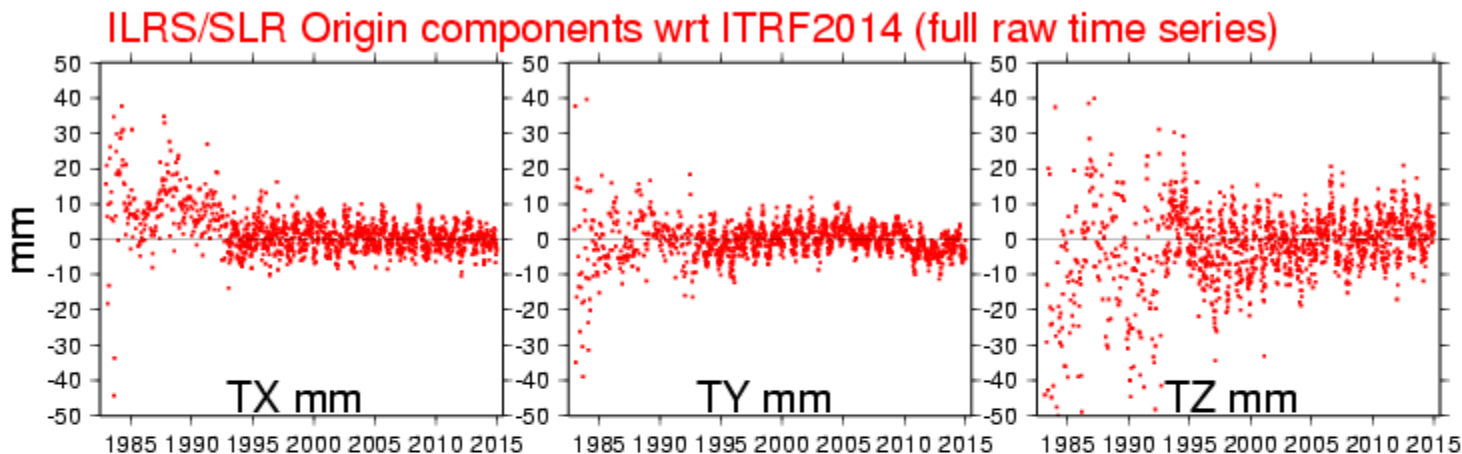
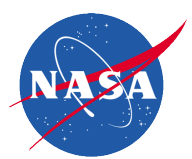


Figure from Zuheir Altamimi, IGN/France  
(Altamimi et al., 2016)



# Annual Geocenter Motion Model



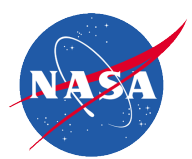
## Annual amplitudes & phases fitted to the SLR translation time series

	X		Y		Z	
	A mm	$\varphi$ deg	A mm	$\varphi$ deg	A mm	$\varphi$ deg
<b>ITRF 2014</b>	<b>2.6</b> $\pm 0.1$	<b>226</b> $\pm 3$	<b>2.9</b> $\pm 0.1$	<b>140</b> $\pm 2$	<b>5.7</b> $\pm 0.2$	<b>208</b> $\pm 2$
<b>ITRF 2008</b>	<b>2.6</b> $\pm 0.1$	<b>222</b> $\pm 3$	<b>3.1</b> $\pm 0.1$	<b>135</b> $\pm 2$	<b>5.5</b> $\pm 0.3$	<b>202</b> $\pm 10$

from Zuheir Altamimi, IGN/France (Altamimi et al., 2016)

We model the geocenter explicitly in Precise Orbit Determination for Altimeter Satellites and get better agreement between SLR+DORIS & GPS Orbits on Jason-2.

(See Melachroinos et al., Adv. Space Res., 2013, doi 10.1016/j.asr.2012.06.004 for details)



# DORIS, SLR & VLBI scales wrt ITRF2014

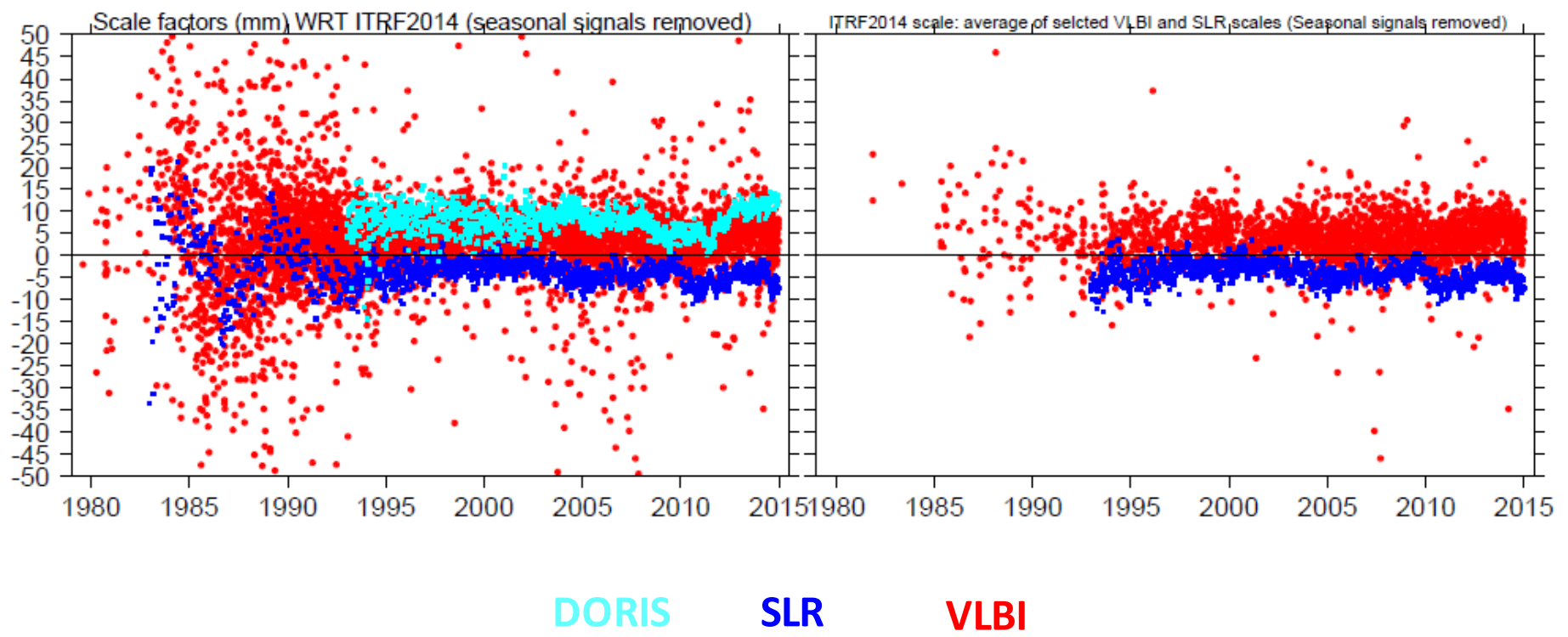
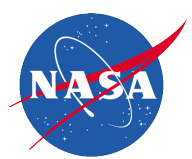


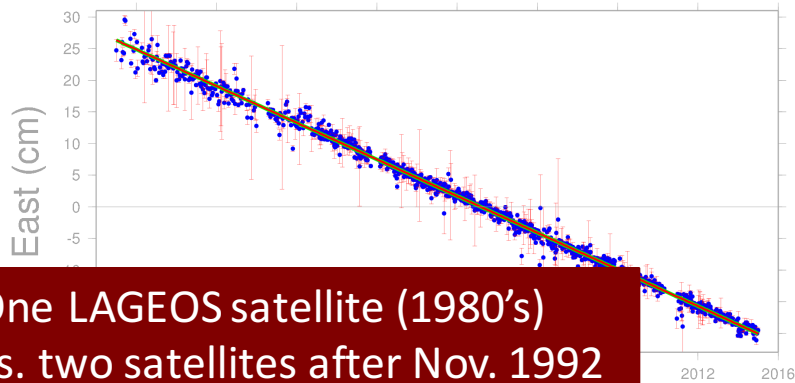
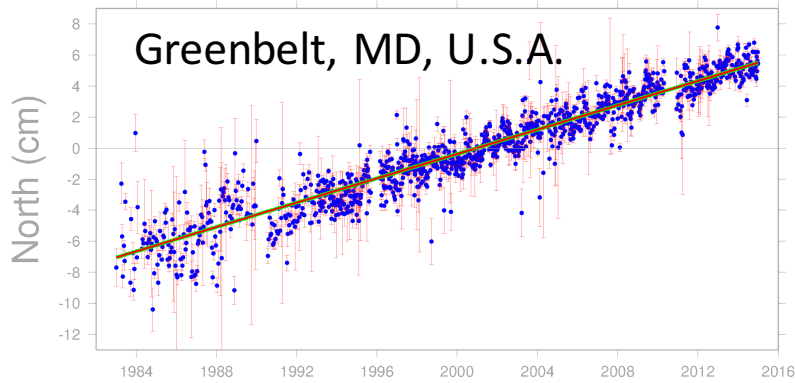
Figure from Zuheir Altamimi, IGN/France (Altamimi et al., 2016)



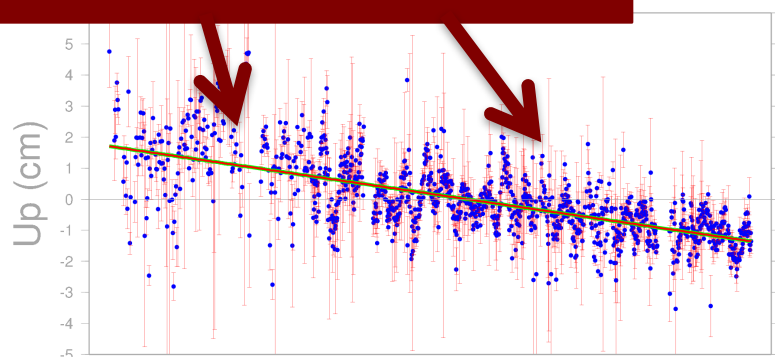
# ITRF2014: SLR station history



7105\_40451M105 trajectory

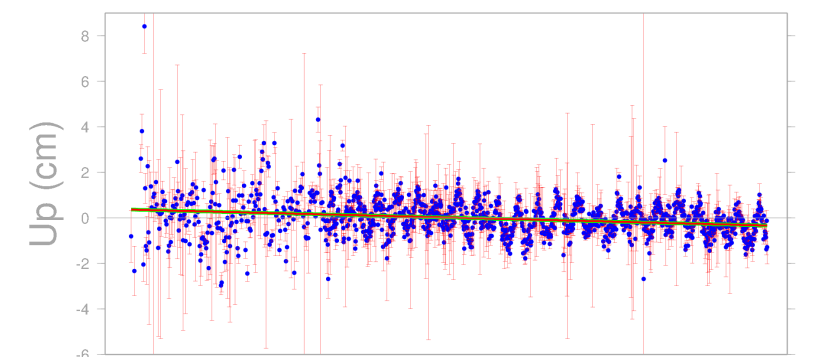
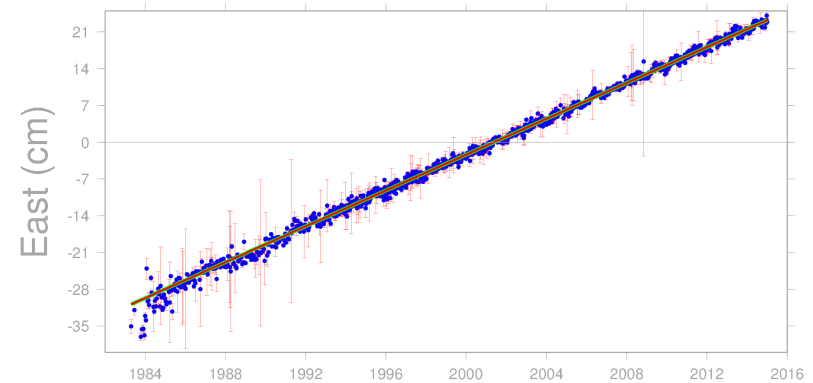
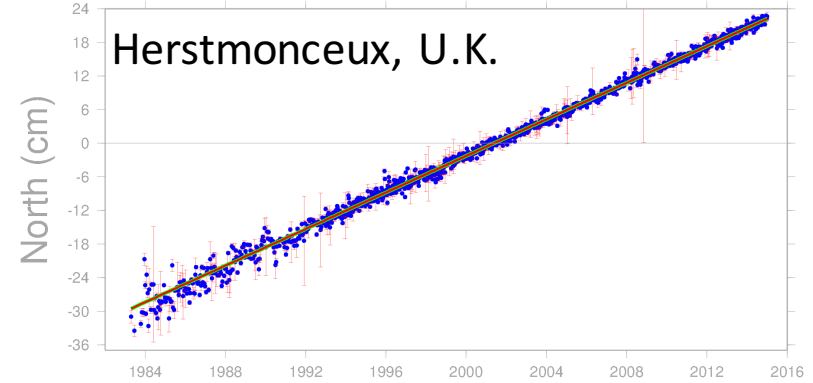


One LAGEOS satellite (1980's)  
vs. two satellites after Nov. 1992



Trajectory: Blue: Raw, Green: Linear, Red: PSD model  
Vertical gray lines represent discontinuities

7840\_13212S001 trajectory



Trajectory: Blue: Raw, Green: Linear, Red: PSD model  
Vertical gray lines represent discontinuities

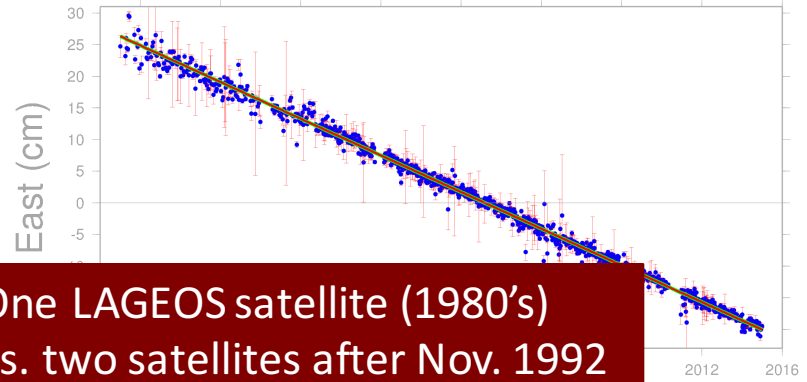
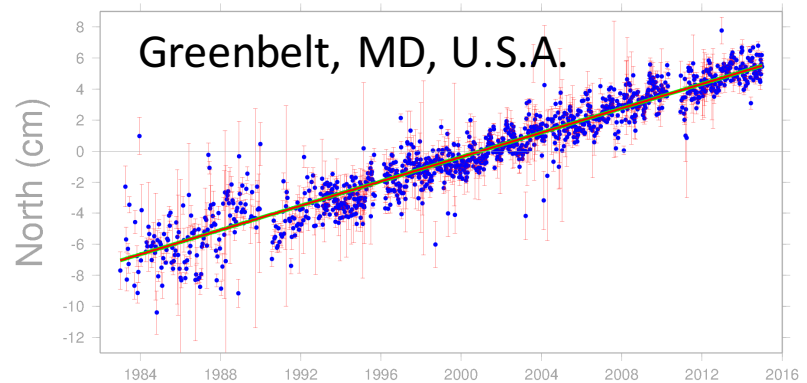




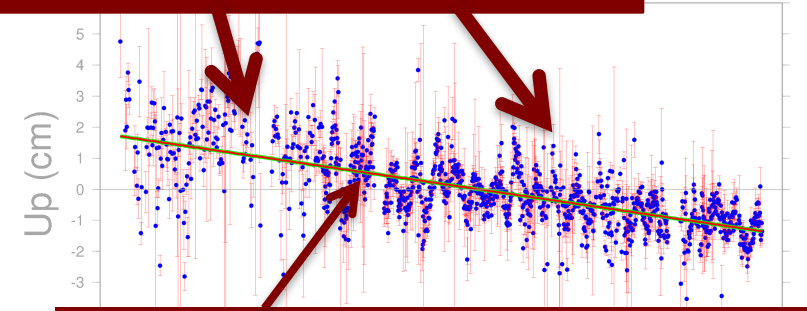
# ITRF2014: SLR station history



7105\_40451M105 trajectory



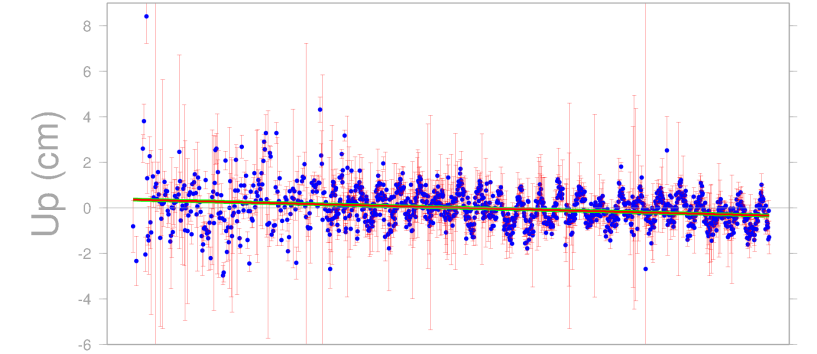
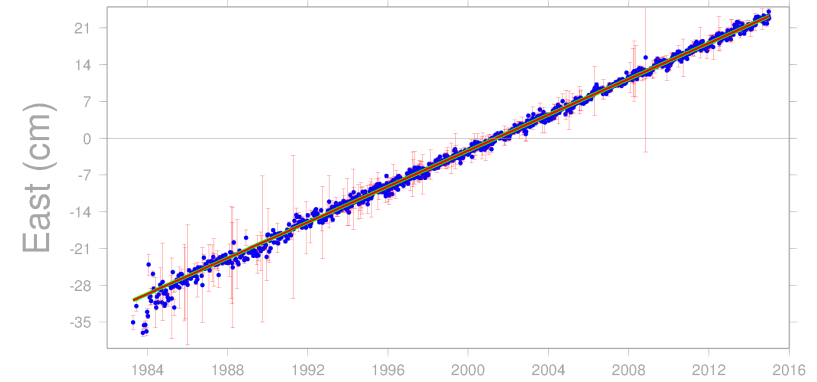
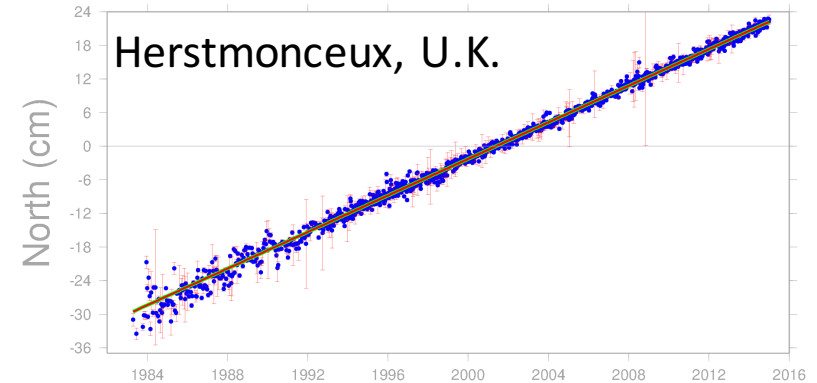
One LAGEOS satellite (1980's)  
vs. two satellites after Nov. 1992



**-3cm / 30 years  $\approx$  -1 mm/yr (GIA signal)**

Vertical gray lines represent discontinuities

7840\_13212S001 trajectory



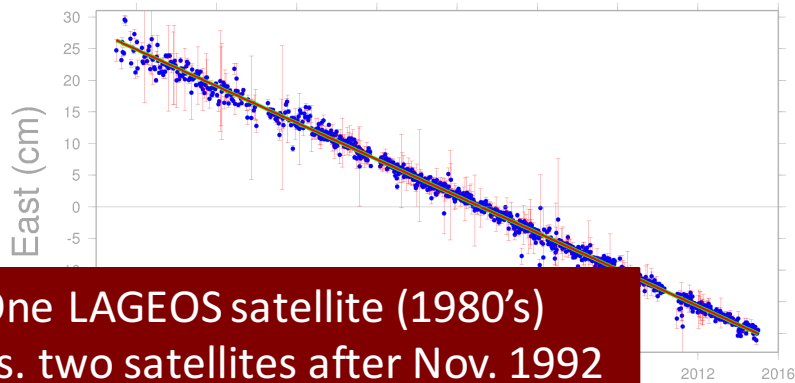
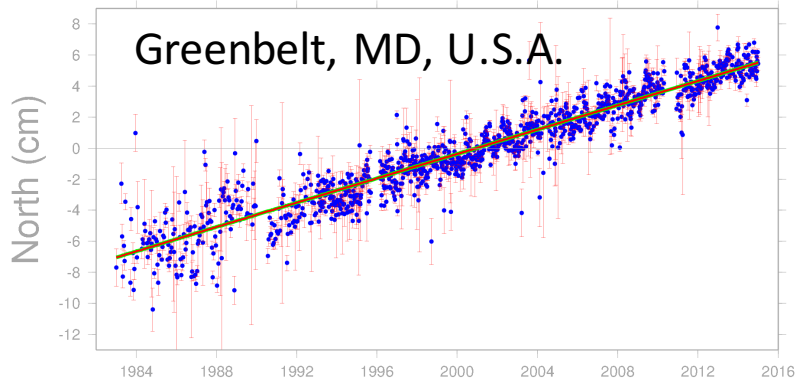
Trajectory: Blue: Raw, Green: Linear, Red: PSD model  
Vertical gray lines represent discontinuities



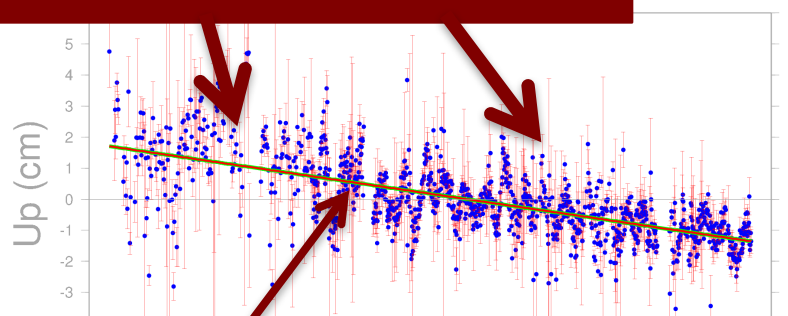
# ITRF2014: SLR station history



7105\_40451M105 trajectory



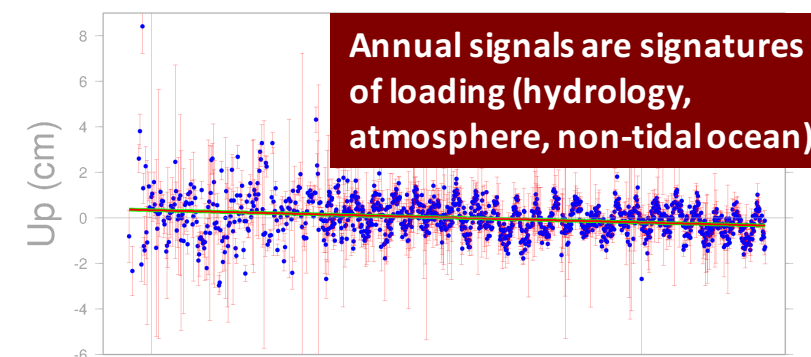
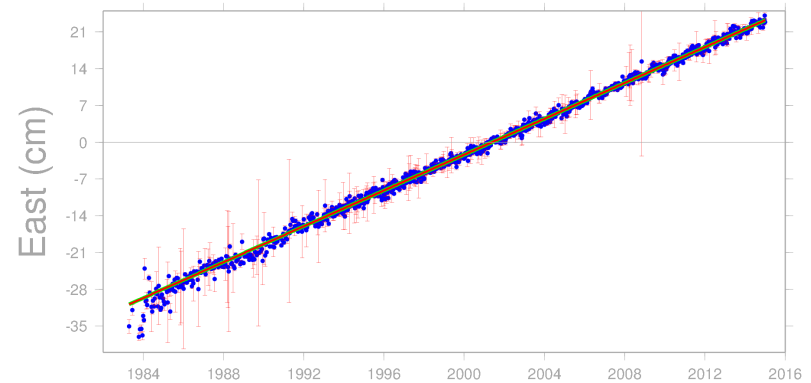
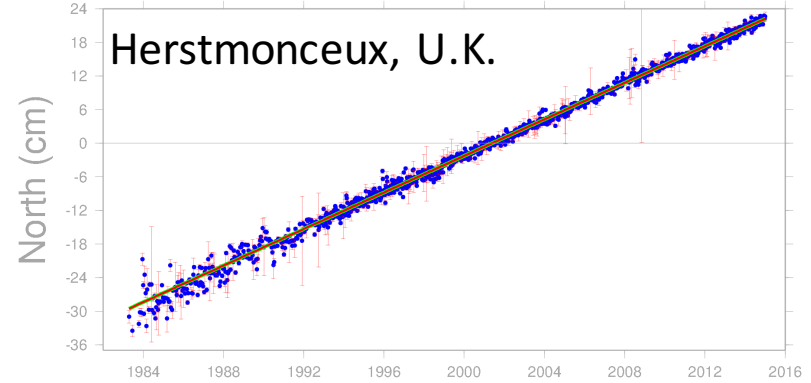
One LAGEOS satellite (1980's)  
vs. two satellites after Nov. 1992



**-3cm / 30 years  $\approx$  -1 mm/yr (GIA signal)**

Vertical gray lines represent discontinuities

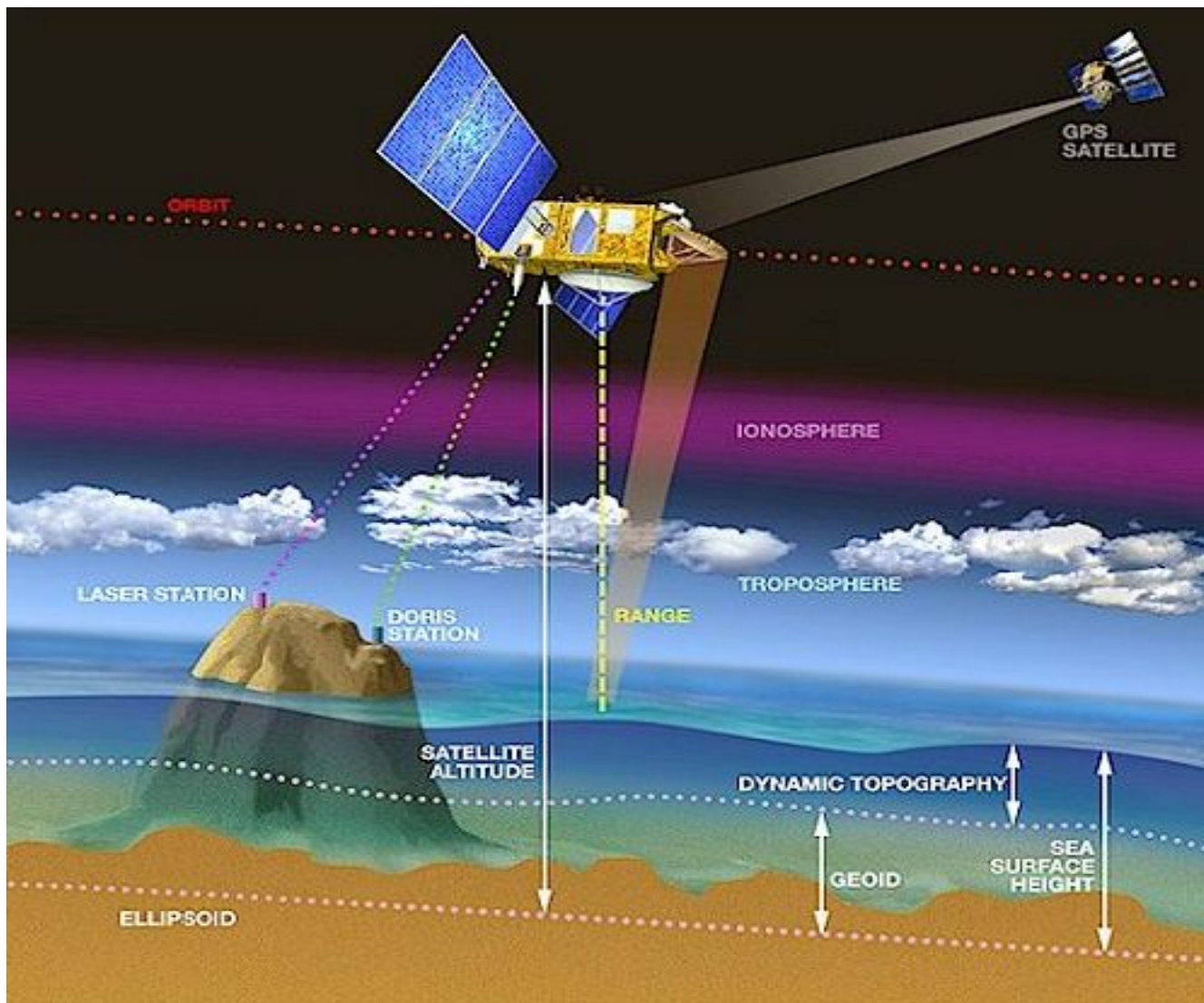
7840\_13212S001 trajectory



Annual signals are signatures  
of loading (hydrology,  
atmosphere, non-tidal ocean)

Trajectory: Blue: Raw, Green: Linear, Red: PSD model  
Vertical gray lines represent discontinuities

# POD - Schematic

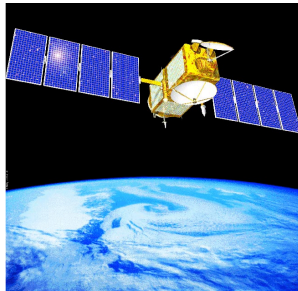


# Altimeter Satellites

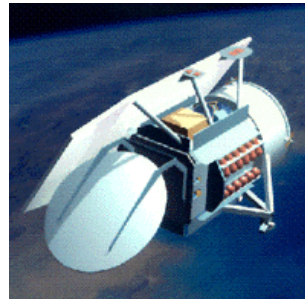
- **SLR data** (provided by stations whose positions were determined by SLR tracking of LAGEOS 1 & 2) **anchor the altimeter satellite orbits in the ITRF.**
- **SLR data are also essential for orbit validation for all missions.**



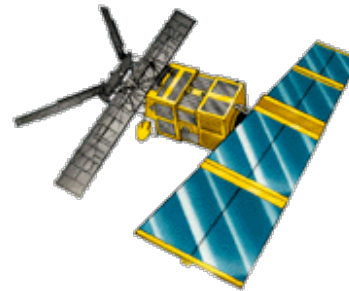
**TOPEX/Poseidon**  
1992



**Jason-1, 2002**  
**Jason-2, 2008**  
**Jason-3, 2016**



**GFO, 1998**



**ERS-1, 1991**  
**ERS-2, 1995**



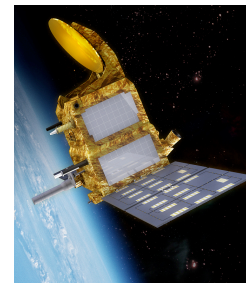
**ENVISAT, 2002**



**CRYOSAT-2, 2010**



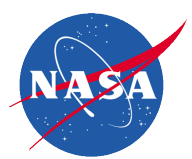
**HY-2A, 2011**



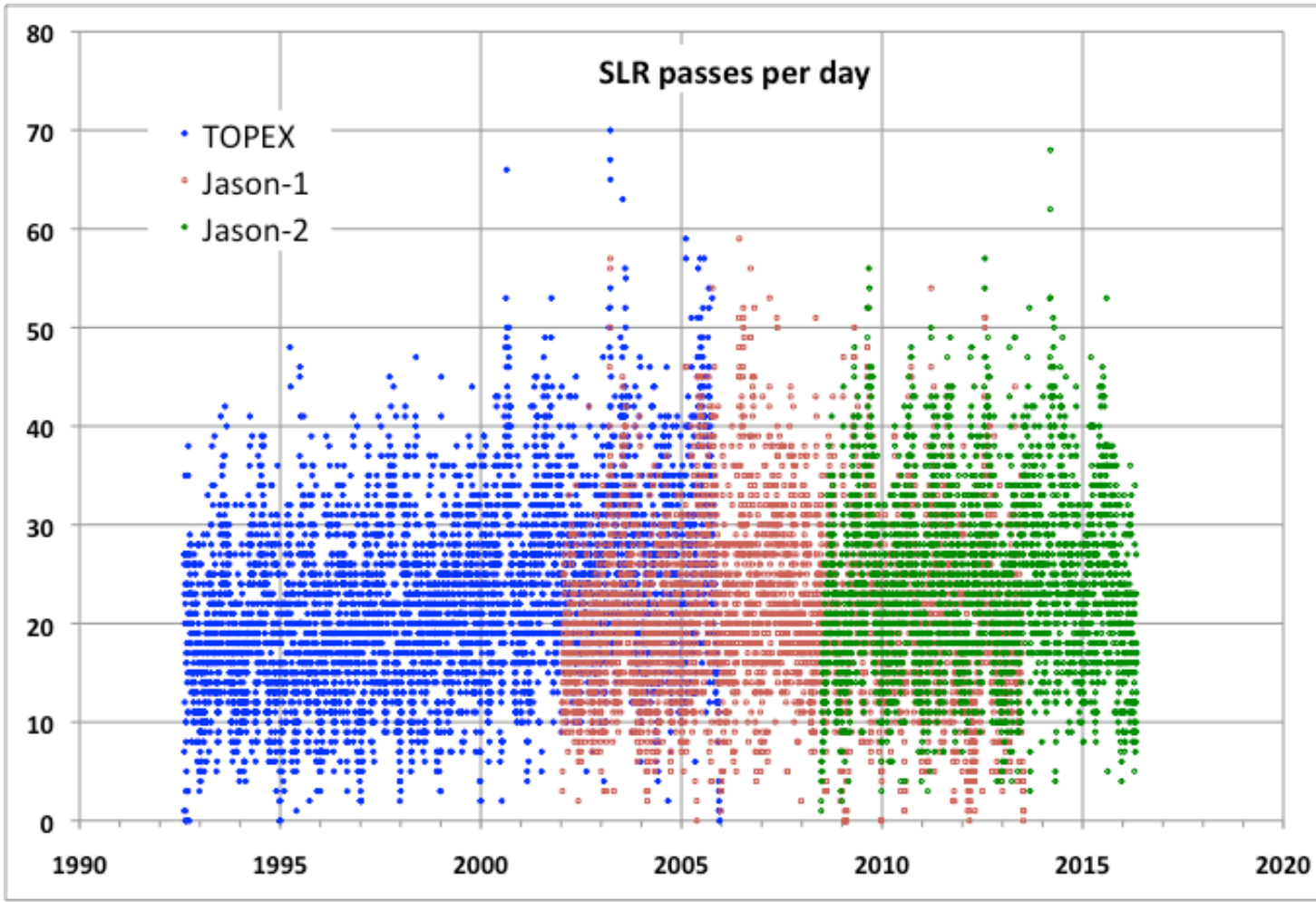
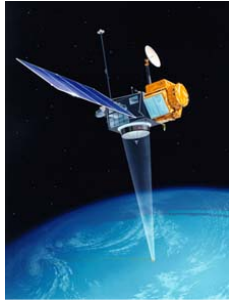
**Saral, 2013**



**ICESAT-1, 2003**



# SLR – TP, J1, J2 tracking summary



# SLR – RMS of fit (TP, J1, J2)

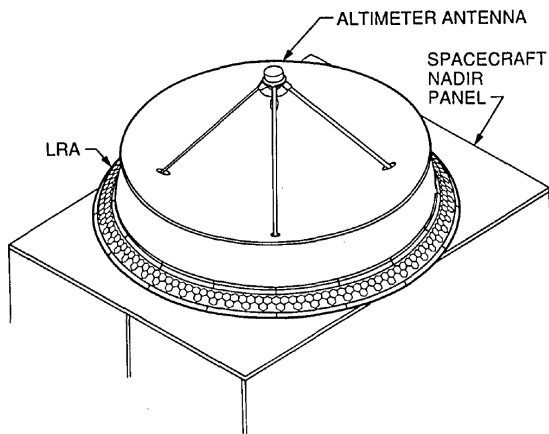
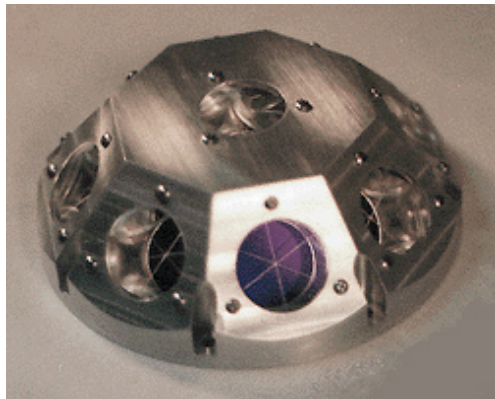
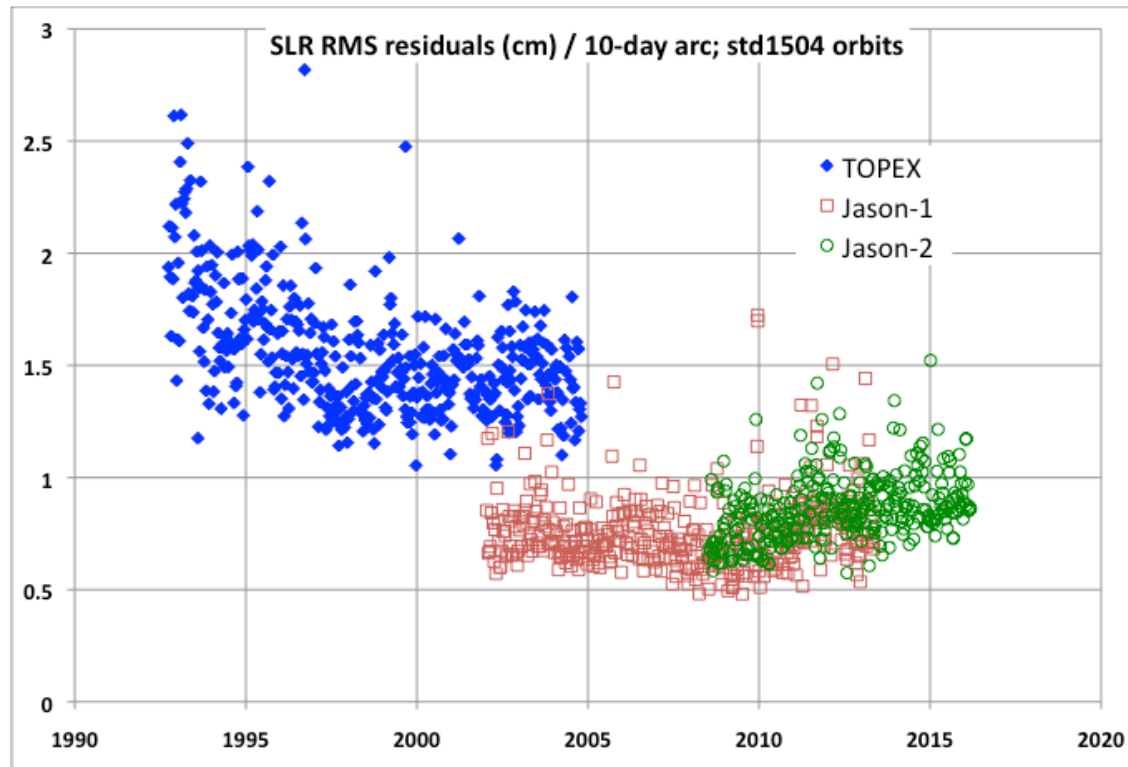


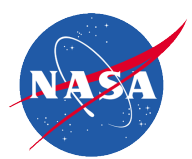
Fig. 1. TOPEX nadir panel with LRA and altimeter antenna.

**TOPEX LRA.**  
(Schwartz, Applied Optics, 1990)

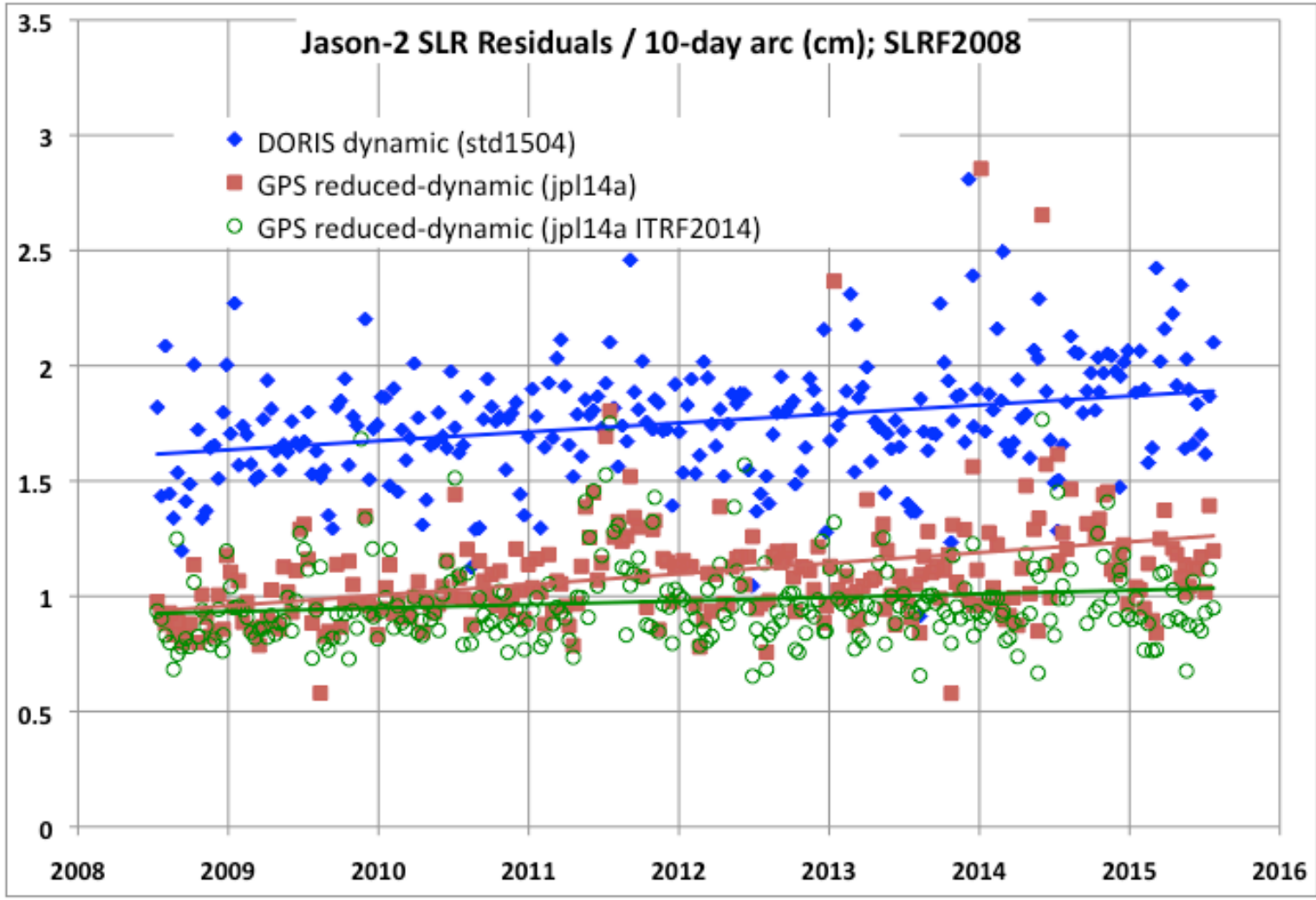


LRA for Jason-1, Jason-2, Jason-3  
(courtesy of the ILRS)

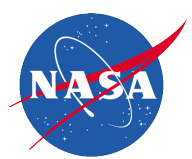




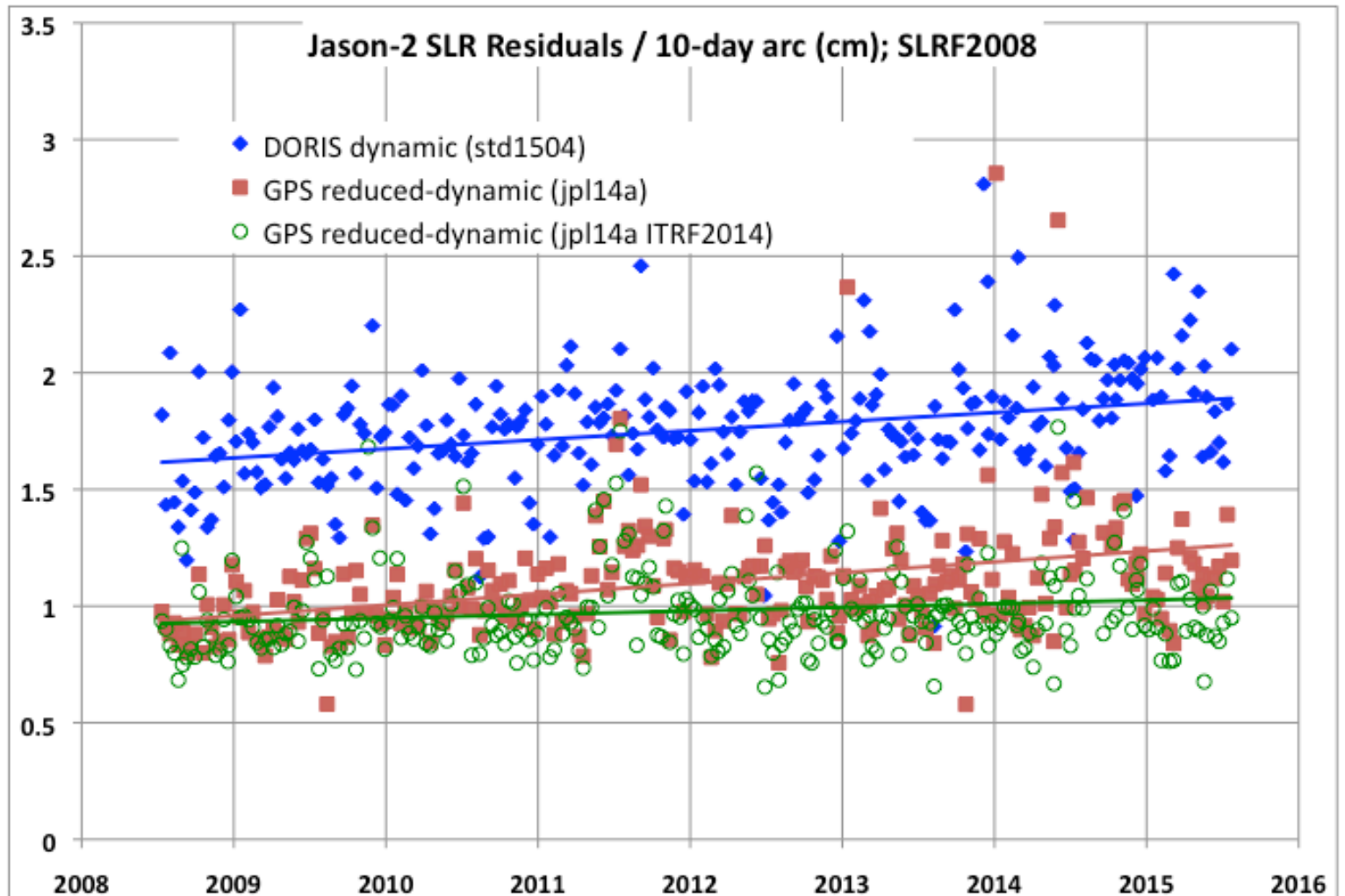
# SLR – Validation of Jason-2 GPS & DORIS orbits



**RMS of SLR fit per Jason-2 10-day cycle for DORIS-only (NASA GSFC) and GPS-only (JPL) Jason-2 orbits**

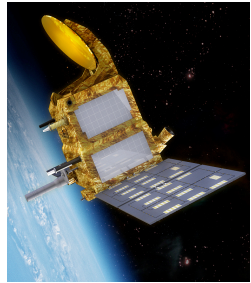


# SLR – Validation of Jason-2 GPS & DORIS orbits

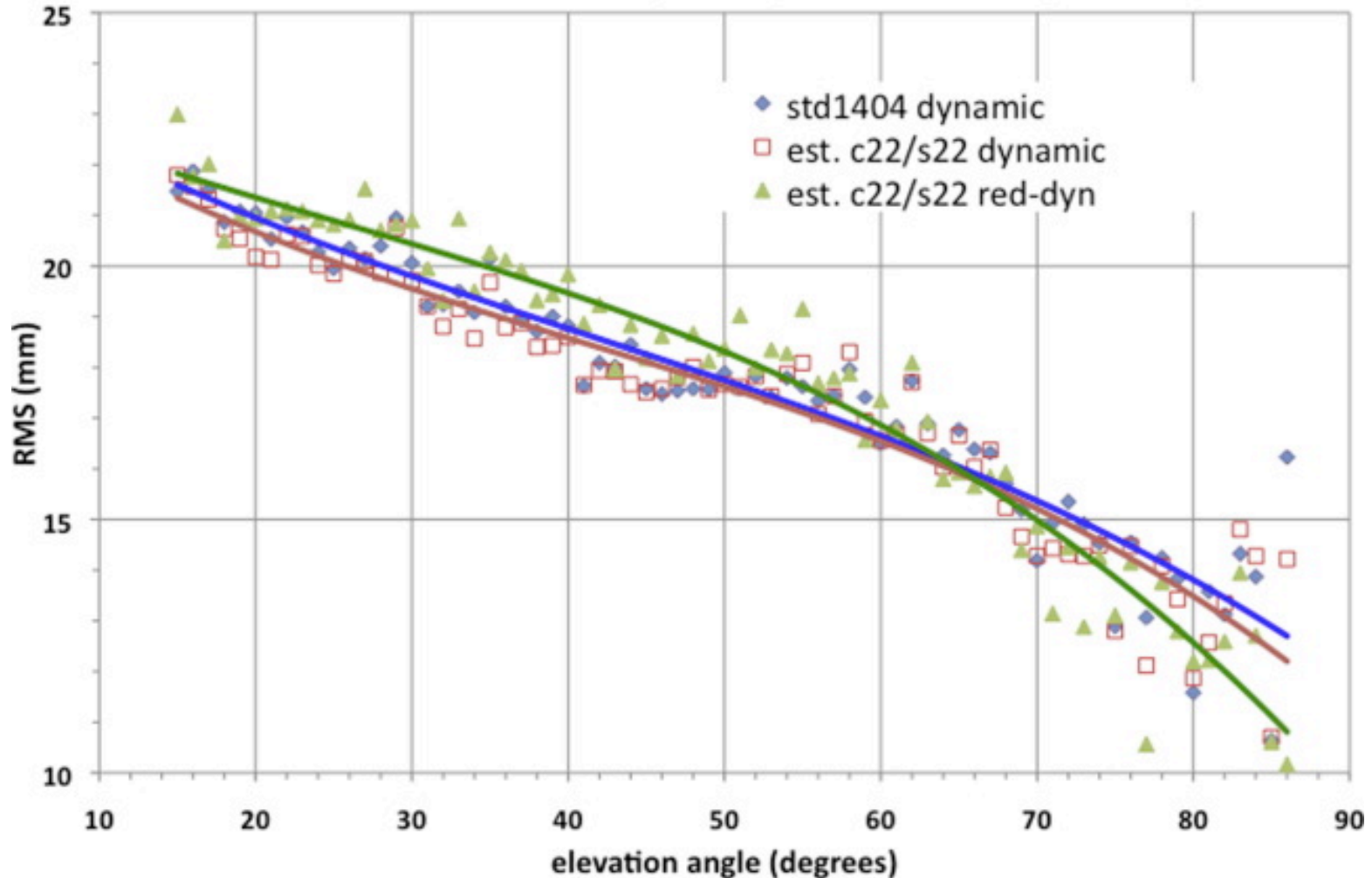


The fact that these orbits from different tracking systems agree at  $\sim 1$ cm radial RMS, is a reason why we can have such high confidence in the determination of Mean Sea Level change from satellite altimetry.





Saral SLR residuals DORIS-only orbits (March 2013 - August 2014)

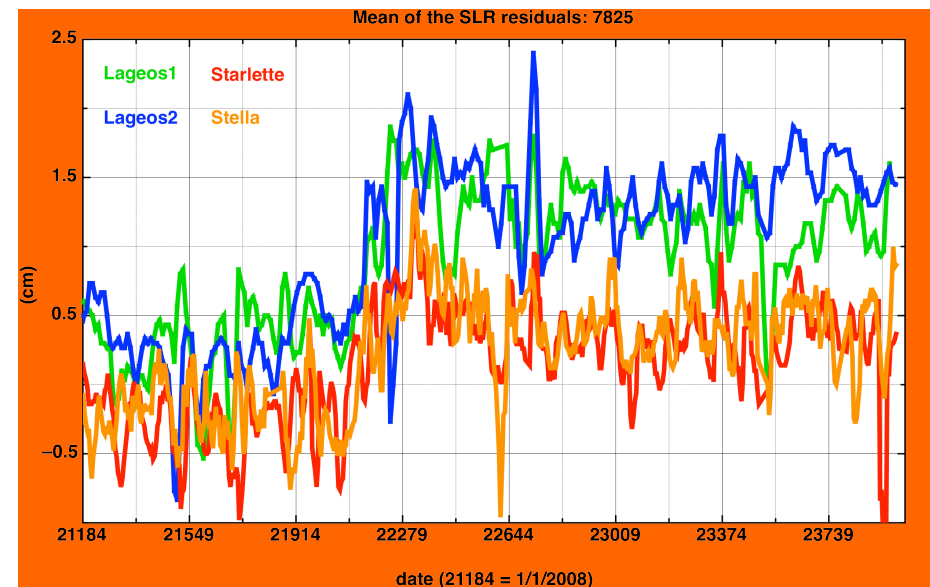
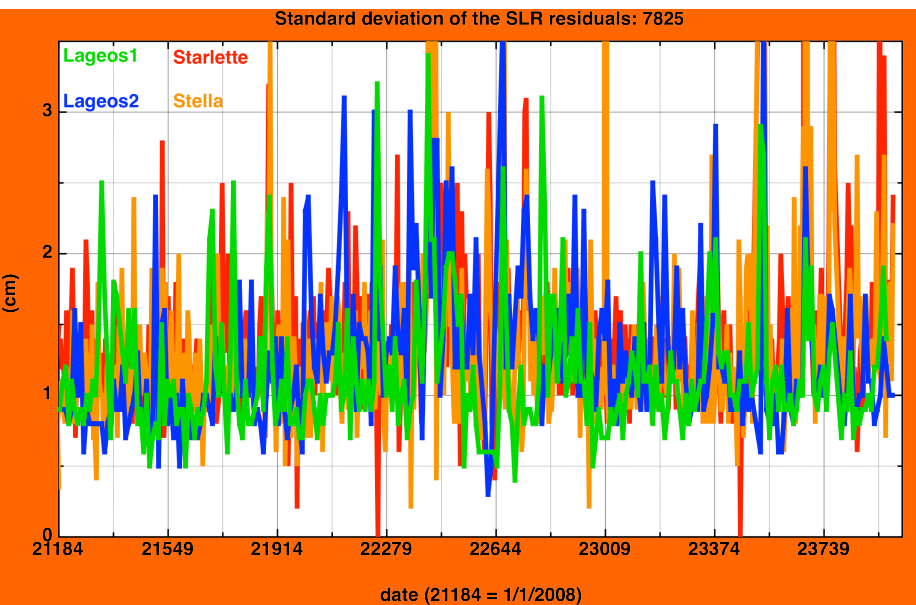


(Zelensky et al., 2016, "Towards the 1-cm SARAL orbit", Adv. Space Res, doi: 10.1016/j.asr.2015.12.011)



# Monitor SLR station Performance for Altimeter Satellites

- Use Data From L1, L2, Starlette, Stella.
- Monitor RMS of Fit, & Mean of Residuals.
- Bruinsma et al. (OSTST, Reston, 2015) reported results on analyses with ITRF2008; 5 day arcs (St/SL), 10-day arcs (L1,L2) – Example below is Mt. Stromlo.



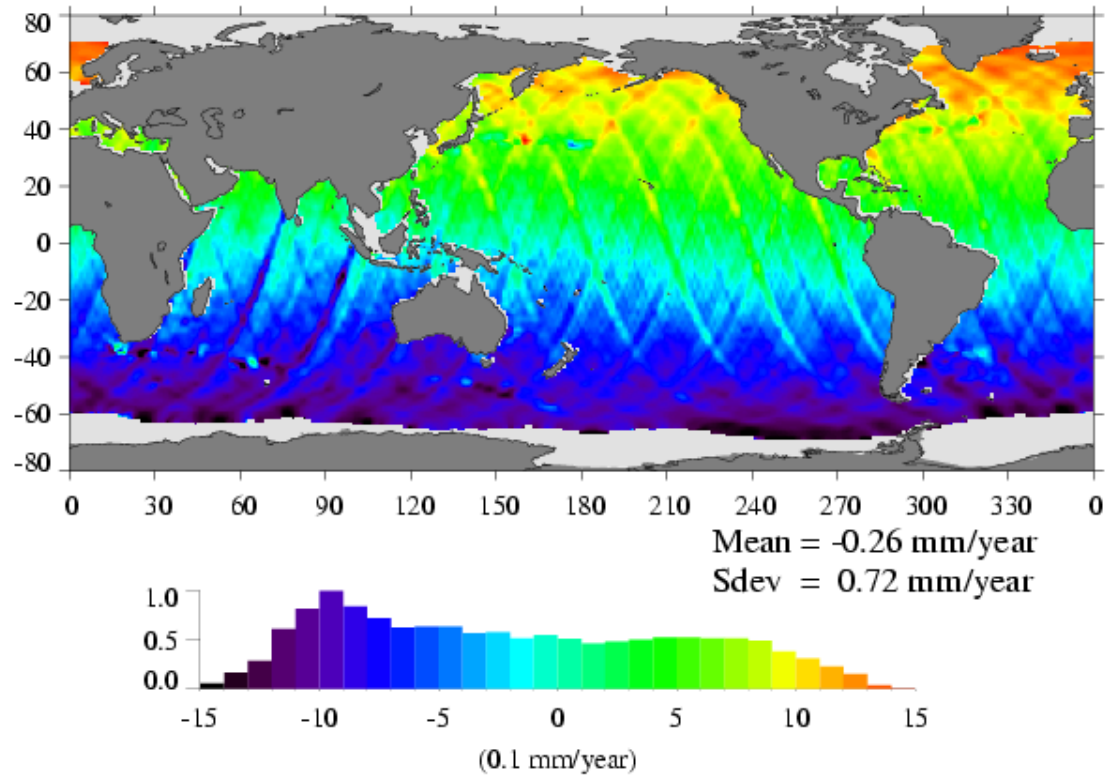
Is there an event timer issue with Mt. Stromlo starting in 2011? We need to repeat this evaluation with ITRF2014.

**Comment: No aberrant residuals observed in development of ITRF2014 (ZA, le 10 mai 2016)**

Reference Frame  
Realizations used in  
Altimeter Satellite POD.

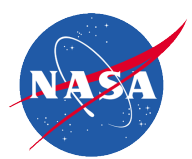
- **CSR95**
- **ITRF2000**
- **ITRF2005**
- **ITRF2008**

Next. **ITRF2014.**



Regional **TOPEX (1993-2002)** Sea Surface Height Trend differences from direct impact of the **ITRF2005 (GGM02C)** minus **CSR95 (JGM3)** orbit differences. (from **Beckley et al., Geophys. Res. Lett., 2007**).

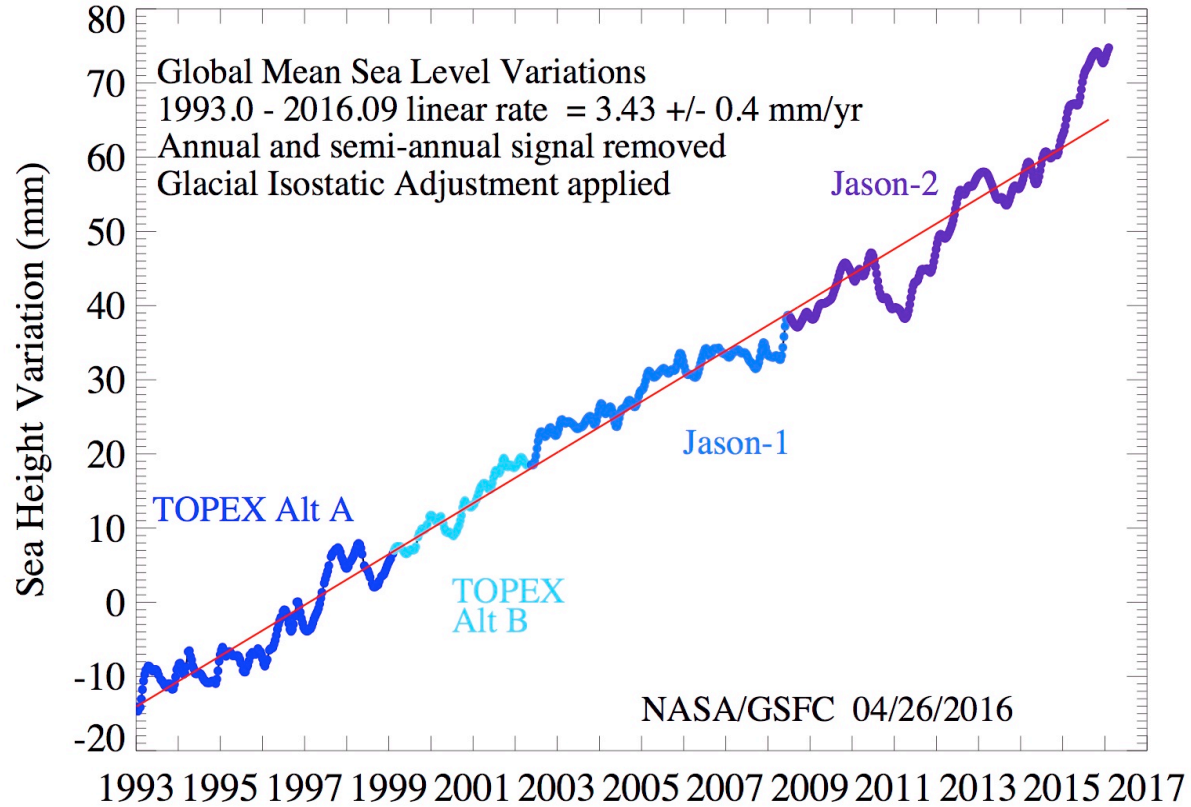
Errors in the Z component of the TRF can produce large regional errors in MSL rate determination.



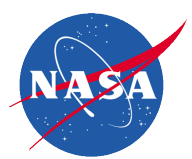
# Altimeter satellites – MSL determination



The precise orbits for TOPEX/Poseidon, Jason-1, Jason-2, all computed in a consistent reference frame (ITRF2008) are used to compute the global change in mean sea level from satellite ocean radar altimeter data.



[http://podaac.jpl.nasa.gov/Integrated\\_Multi-Mission\\_Ocean\\_AltimeterData](http://podaac.jpl.nasa.gov/Integrated_Multi-Mission_Ocean_AltimeterData)



# I-What about LAGEOS “constellations”?

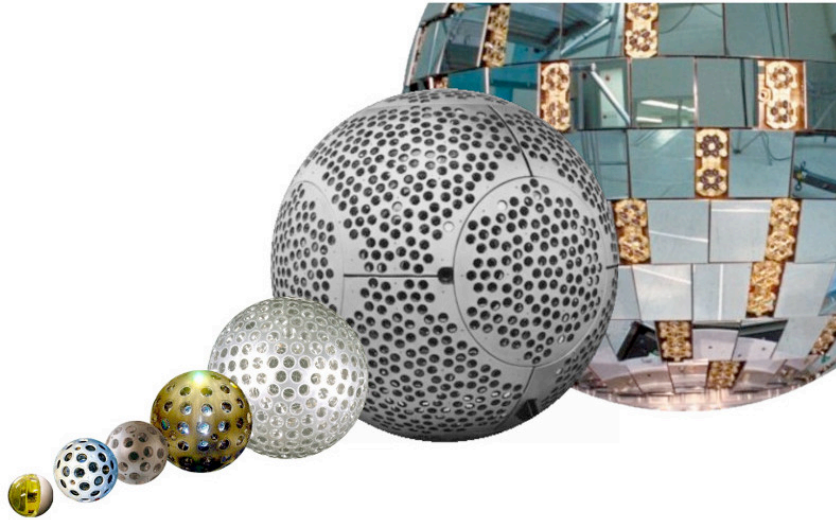
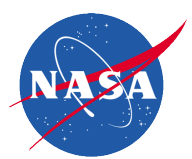


Figure courtesy of SGF/Herstmonceux

We have a suite of passive ‘geodetic’ satellites that orbit the Earth and are precisely tracked by Satellite Laser Ranging.

We have a “de facto” constellation, and these satellites have contributed to estimations of time-variable gravity as well as drag studies.

Can they also contribute to the TRF?



# II-What about LAGEOS “constellations”?

Altitude (km)	Satellite	1985	1990	1995	2000	2005	2010	2015	
5850	Lageos1	[Green bar from 1985 to 2015]							
5625	Lageos2	[Green bar from 1990 to 2015]							
1472	Ajisai	[Green bar from 1985 to 2015]							
1450	Lares	[Green bar from 2010 to 2015]							
958*	Starlette	[Green bar from 1985 to 2015]							
832	Blits	[Green bar from 2010 to 2015]							
780	Stella	[Green bar from 1990 to 2015]							
691	Larets	[Green bar from 2005 to 2015]							

\* Starlette: Elliptical orbit (~800 x ~1100 km)

**アジサイ**

(Ajisai)

hydrangea

318 mirrors, 1436 CCRs



**Starlette:**

Satellite de Taille Adaptée avec Réflecteurs Laser pour les Etudes de la Terre

**Starlette & Stella:**

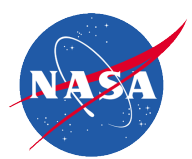
noyau. U-238

+ 1,5% Mb (Starlette),

+ 0.2% V (Stella);

Surface: Al (20 facettes, 3 CCRs each)

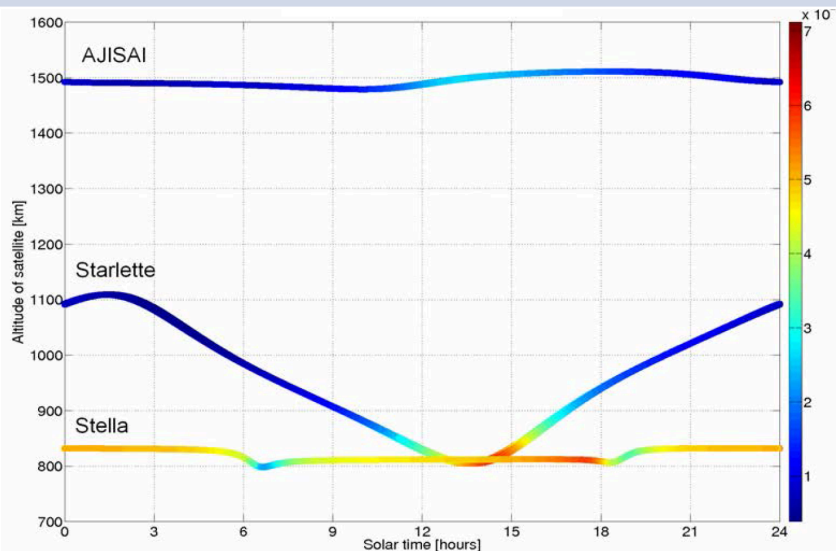




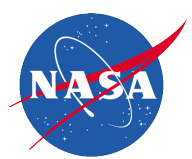
# III-What about LAGEOS “constellations”?

Satellite	Altitude	Diameter	A/m (10 <sup>-4</sup> m <sup>2</sup> /kg)	Mass (kg)
LAGEOS 1,2	5850, 5625	60 cm	7.0	407; 405
<b>Ajisai</b>	<b>1472</b>	<b>2.15 m</b>	<b>53.0</b>	<b>685</b>
LARES	1450	36 cm	2.7	386.8
<b>Starlette/Stella</b>	<b>958, 780</b>	<b>24 cm</b>	<b>~9.6</b>	<b>47.5; 48</b>
Blits	832	17 cm	30.1	7.5
Larets	691	21 cm	14.9	23.3

[see Bloßfeld (2015, J. Geodesy, Table 2) & Sosnica (2014, J. Geodesy) & ILRS web site (<http://ilrs.gsfc.nasa.gov>) for a more detailed list.]



Drag Accelerations on **Starlette, Stella and Ajisai**  
 (from Sosnica, Ph.D Thesis, AIUB, 2014)



# IV-What about LAGEOS “constellations”?

Satellite	Altitude	Diameter	A/m (10 <sup>-4</sup> m <sup>2</sup> /kg)	Mass (kg)
LAGEOS 1,2	5850, 5625	60 cm	7.0	407; 405
<b>Ajisai</b>	<b>1472</b>	<b>2.15 m</b>	<b>53.0</b>	<b>685</b>
LARES	1450	36 cm	2.7	386.8
<b>Starlette/Stella</b>	<b>958, 780</b>	<b>24 cm</b>	<b>~9.6</b>	<b>47.5; 48</b>
Blits	832	17 cm	30.1	7.5
Larets	691	21 cm	14.9	23.3

[see Bloßfeld (2015, J. Geodesy, Table 2) & Sosnica (2014, J. Geodesy) & ILRSweb site (<http://ilrs.gsfc.nasa.gov>) for a more detailed list.]

## Three issues:

### **(1) Nonconservative forces.**

(Drag, Solar Radiation, Planetary Radiation Pressure)

### **(2) Pass Length (Amount of data).**

### **(3) Target Signature effects.**

-> cannot be ignored for mm geodesy!!

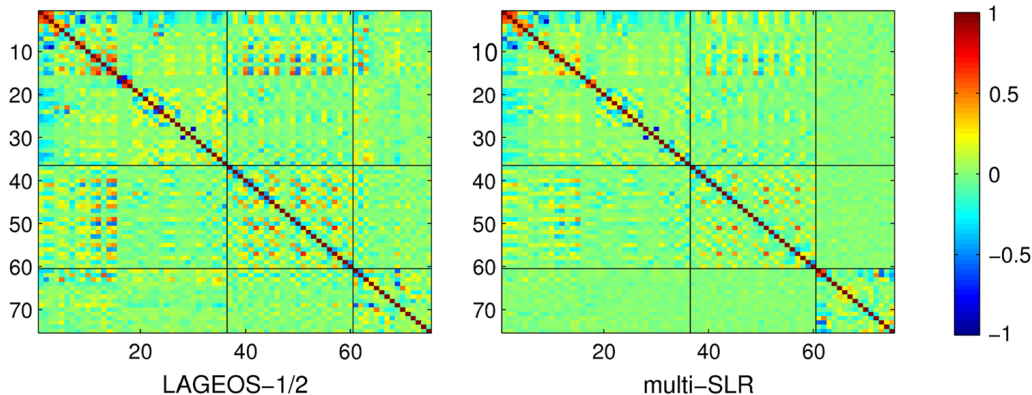
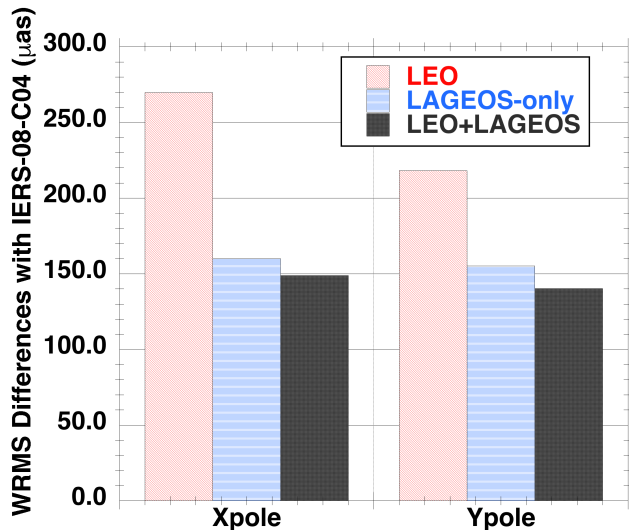
- Otsubo & Appleby, *JGR*, 2003; LAGEOS & Ajisai.
  - Otsubo et al., *J. Geodesy*, 2015
- Starlette, Stella, LARES.





# V-What about LAGEOS “constellations”?

- Sosnica (J. Geodesy, 2014) looked at the contribution of adding Starlette, Stella + Ajisai to the TRF weekly solutions.

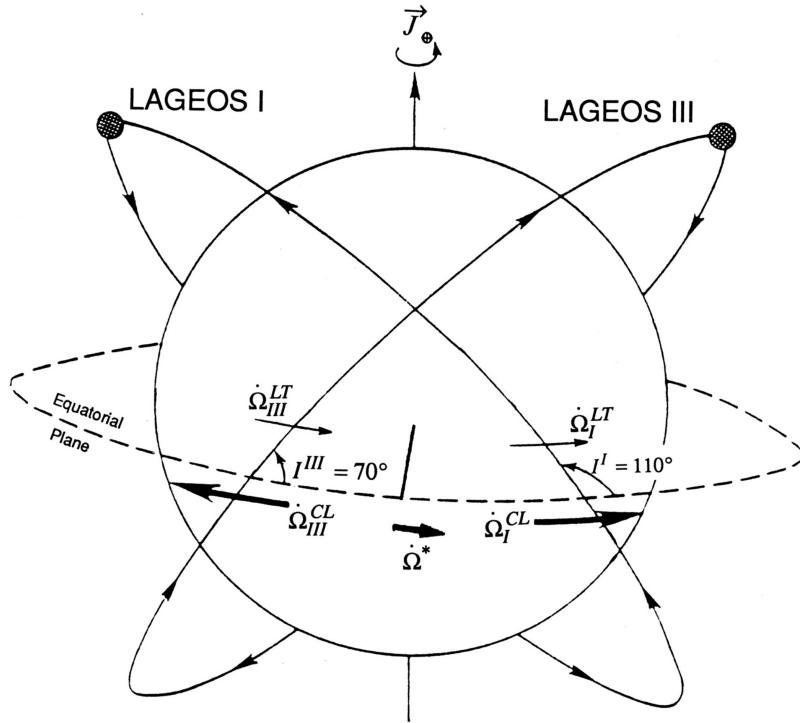
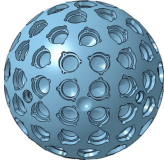


- Only a small improvement for EOP.

Fig 12. Sosnica (J. Geodesy, 2014). Correlation matrix of weekly solutions, ordered by station coordinates, EOP, gravity.

- Correlations reduced for ‘combination solution’.
- Position determination for stations that have limited SLR data from LAGEOS, are improved.

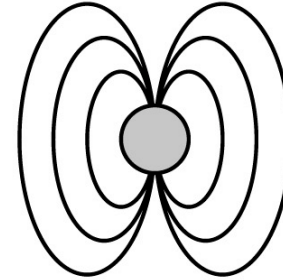
# What about LAGEOS-3?



Object of measurement:

$$\dot{\Omega}^* = \frac{1}{2} (\dot{\Omega}^I + \dot{\Omega}^{III})$$

- **Ciufolini (1986)** proposed a LAGEOS-3 satellite to measure LT.
- A **NASA study (1989)**, Ph.D theses (**Ries, 1992; Petersen 1997**) & other studies explored this idea.



$$\vec{F}_{LT} = m_0 \vec{v} \times \left[ \nabla \times \left( (-1 + \gamma) \frac{G \vec{J}_{cb} \times \vec{r}}{c^2 r^3} \right) \right]$$

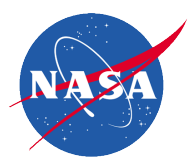
Spinning Mass

Just as a spinning charge produces a magnetic field, a spinning mass produces a “gravitomagnetic” field.

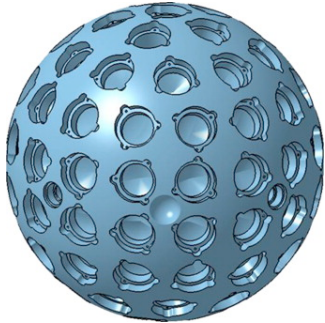
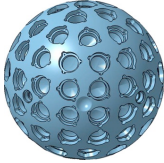
- The most observable effect on the satellite orbit is the Lense-Thirring precession of the ascending node.

$$\dot{\Omega} = \frac{2G}{c^2 a^3} \frac{J}{(1-e^2)^{\frac{3}{2}}}$$

~31 milli-arcsec/yr  
for LAGEOS



# What is LARES?

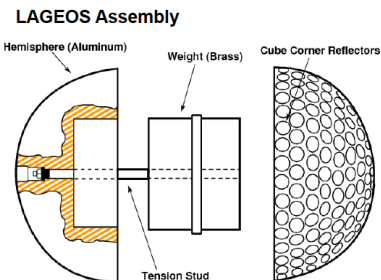
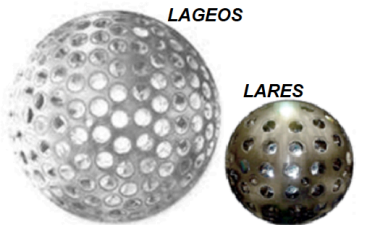


LARES

- Launched in 2012 (Italy).
  - Main objective – measure Lense-Thirring effect.
  - Built with a high-density, tungsten alloy (18 gm/cm<sup>3</sup>).
  - Launched on a VEGA qualification flight;
- Target altitude & inclination were a combination of what the launch vehicle could reach, and minimization of error in Lense-Thirring measurement.

## LARES Mission: engineering aspects

Design: LARES vs LAGEOS



	LAGEOS	LARES
Launch:	• 1976 (1) • 1992 (2)	2012
Mass:	• 406.9 kg (1) • 405.3 kg (2)	386.8 kg
Diameter:	60 cm	36.4 cm
Body:	Assembly.	Single piece.
No. of CCR:	426	92
Eccentricity:	• 0.0045 • 0.0135	0.0002
Altitude:	• 5860 km (1) • 5620 km (2)	1450 km

## Impact of LARES on TRF

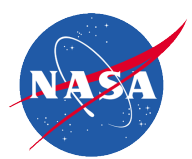
(ie. LARES + LAGEOS-1,2)

**Stations: Improve by 17-20%.**

**EOP: Improve by 20-23%.**

**(Preliminary results from E. Pavlis)**

Figure from Pavlis et al., 2015



# Summary



- The LAGEOS satellites are of immense importance for the ITRF since they are the means by which the origin of the reference frame is determined.
- The SLR stations – whose positions are determined by LAGEOS data – anchor all radar and laser altimeter data in the ITRF; Their data is also used for orbit validation.
- The determination of mean sea level on a global and regional basis have depended on the SLR contribution to the ITRF and hence directly on LAGEOS data.
- The addition of a “LAGEOS-2” had a profound impact on the determination of the station coordinates and the geocenter.
- Studies have proposed (e.g. Ciufolini et al., IAF, 2015) to launch a LARES-2 s/c to low altitude (1450 km), or to a LAGEOS-type altitude (but a supplementary inclination). The benefit for the TRF should be seriously evaluated.  
(For DORIS the addition of new LEO satellites at new inclinations has each time improved the determination of the TRF parameters – see Moreaux et al., Adv Space Res, 2016).

## Acknowledgements:

Zuheir Altamimi (IGN, France); Richard Biancale (CNES/GRGS)  
Carey Noll (NASA GSFC); Erricos Pavlis (UMBC @ NASA GSFC);  
Nikita Zelensky (SGT @ NASA GSFC);

